## Microeconomics 1 – Part A: Individual decision making Masters M1 IMMAEF & MAEF

## TD – Monday, October 16, 2023

## **Consumer Theory**

The following exercise should be submitted on Monday, October 16.

**Exercise.** Let  $X := (-\infty, \infty) \times \mathbb{R}^{L-1}_+$  be the consumption set. The consumer has continuous, strictly convex preferences on X that are represented by a utility function

$$u(x) = x_1 + \varphi(x_2, x_3, \dots, x_L)$$

We assume  $p \gg 0$  and we normalize  $p_1 = 1$ .

- 1. Show that the demand for commodities  $\{2, 3, ..., L\}$  must be independent of wealth. How does demand for commodity 1 react to changes in wealth w?
- 2. Using your previous result, define the **indirect utility function v as usual**, that is, for every  $(p, w) \in \mathbb{R}^{L+1}_{++}$ ,

$$v(p, w) := u(x^*)$$
 with  $x^* \in x(p, w)$ 

Show that v(p, w) is linear in wealth and  $v(p, w) = w + \psi(p)$  for some function  $\psi : \mathbb{R}_{++}^L \to \mathbb{R}$ .

3. Now let L=2 and  $\varphi(x_2)=\alpha \ln(x_2)$ . Solve the UMP as a function of (p,w) (Recall that in this exercise we allow demand of commodity 1 to be negative).