

TD – Wednesday, October 23, 2024

Producer Theory

The following exercise should be submitted on Wednesday, October 23.

The **basic properties (BP)** of  $Y$  to be verified are the following ones.

**(BP):** Possibility of inaction, closedness, impossibility of free production (“no free lunch”), free-disposal, convexity, increasing/decreasing/constant returns to scale.

**Exercise.** A firm produces commodity 2 using commodity 1 as an input. The production function is:

$$f(z) = \alpha z \text{ with } \alpha > 0 \text{ and } z \geq 0.$$

1. Determine, both formally and graphically, the production set  $Y$  associated with the production function  $f$ .
2. Determine if the production  $Y$  verifies the basic properties **(BP)**.
3. Answer questions 1) and 2) for the production function:  $f(z) = \alpha\sqrt{z}$  with  $\alpha > 0$  and  $z \geq 0$ .
4. Answer questions 1) and 2) for the production function:  $f(z) = \alpha[1 - \exp(-kz)]$  with  $k > 0$ ,  $\alpha > 0$  and  $z \geq 0$ .